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## **Outline**

## **● Causal Discovery for Time-series Data** ○ PCMCI algorithm

● Robotics Applications **S** F-PCMCI algorithm **≮ CAnDOIT algorithm CausalFlow** & ROS-Causal

The PC and FCI causal discovery methods work well with discrete/categorical data.

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#### **example**

non-smoker **0** - smoker **1** age under 50 **0** - age over 50 **1** no lung cancer **0** - lung cancer **1**



#### **The order is not important**



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#### **What if our data is time-dependent?**



The PC and FCI causal discovery methods work well with discrete/categorical data.

#### **What if we deal with time-series data?**

PC/FCI is inappropriate to use with time series data due to:

- time ordering
- lagged dependencies
- high false positive rates due to the autocorrelation.

$$
\begin{cases}\nX_t^0 = 0.2(X_{t-1}^1)^2 + \eta_t^0 \\
X_t^1 = \eta_t^1 \\
X_t^2 = 0.3(X_{t-2}^1)^2 + \eta_t^2\n\end{cases}
$$

$$
\begin{pmatrix}\n\frac{1}{2} & \frac{1}{2} & \
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It consists of two main steps:

#### ● **PC algorithm**

retrieves the causal model structure by considering ONLY lagged dependencies as possible causal relationships between variables

#### **● MCI test**

validates the structure found at the previous step by performing a false positive rate optimisation control

 $X_{t-\tau}^i \perp \!\!\! \perp X_t^j | \tilde{P}(X_{t-\tau}^i), \tilde{P}(X_t^j) |$ 

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## **● Robotics Applications**

- **S** F-PCMCI algorithm
- **≮ CAnDOIT algorithm**
- **CausalFlow**
- & ROS-Causal

### Robotics Applications

Main challenges in robotics:

- execution time of the causal discovery analysis
- conduct causal discovery using data from observations and interventions
- conduct the causal discovery analysis online



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## Robotics Applications  $\rightarrow$  F-PCMCI algorithm

PCMCI computational cost depends on:

- the length of the time-series
- the number of variables

Filtered-PCMCI (**F-PCMCI**) steps:

- takes in input a prefixed set of variables
- the Transfer Entropy-based filter analyses and removes irrelevant variables (e.g., constants or isolated ones). The reduced variable set is used to create a hypothetical causal model
- the hypothetical causal model needs to be validated by a proper causal analysis, which is performed by PCMCI

#### This strategy enables **faster** and **more accurate** causal discovery



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\begin{cases} x_0(t) = 2x_1(t-1) + 3x_3(t-1) + \eta_0 \\ x_1(t) = \eta_1 \\ x_2(t) = 1.1x_1(t-1)^2 + \eta_2 \\ x_3(t) = x_3(t-1) \cdot x_2(t-1) + \eta_3 \\ x_4(t) = x_4(t-1) + x_5(t-1) \cdot x_0(t-1) + \eta_4 \\ x_5(t) = \eta_5 \\ x_6(t) = \eta_6 \end{cases} \in \mathsf{F}.
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$$
Isolated



Considering the interaction scenario modelled by three variables

- $v_{ii}$ : relative velocity between agent i and j
- $d_{ii}$ : distance between agent i and j
- theta $\alpha$  angle between agent i and j

**Are all the observable variables useful to understand the observed scenario?**







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● Observational data alone are often insufficient to accurately identify the correct causal model in complex scenarios where not all variables are observable

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Causal model obtained by using **Latent-PCMCI (LPCMCI)**: version of PCMCI, based on FCI, that handles latent variables



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Despite the "simple" toy problem (linear, 4 variables)

- reconstructing the causal model from data is never straightforward
- especially when there are hidden confounders

Causal model obtained by using **Latent-PCMCI (LPCMCI)**: version of PCMCI, based on FCI, that handles latent variables



How can we perform causal discovery using data from observations  $\odot$  and interventions  $\triangle$  ?

- Observational data alone are often insufficient to accurately identify the correct causal model in complex scenarios where not all variables are observable
- We need **interventions**

**CAnDOIT: CAusal Discovery with Observational @ and Interventional < data from Time-series** 



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#### **CAnDOIT: CAusal Discovery with Observational © and Interventional & data from Time-series**



- For the observational case, we need to consider B's parents
- For the interventional case, we need to remove all incoming links to B

**How can we enable a causal discovery method to do this?**

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Causal model obtained by using **CAnDOIT**



Consider the brightness of the colours of the objects in the cylinder captured by a robot camera



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$$
\int F_c(t) = b(H(t-1))
$$
  
\n
$$
C_c(t) = b(H(t-1), v(t-1), d_c(t-1))
$$
  
\n
$$
b = K_h \frac{H}{H_{max}} + K_v \left(1 - \frac{v}{v_{max}}\right) + K_d \frac{d_c}{d_{c_{max}}}
$$







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pip install py-causalflow

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**SCREED** 



- ROS-Causal extracts and collects data from a HRI scenario, such as agents' trajectories, and performs causal analysis on the collected data in a batched manner. It is composed by four different rosnodes:
	- roscausal\_robot
	- o roscausal human
	- roscausal data
	- roscausal\_discovery

Castri, Luca, et al. "Experimental Evaluation of ROS-Causal in Real-World Human-Robot Spatial Interaction Scenarios" (2024).

#### **ROS-Causal\_HRISim**

HRI simulator involving:

- TIAGo robot
- pedestrians











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#### Reference

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- Castri, L., Mghames, S., Hanheide M. and Bellotto, N. 2024. CAnDOIT: Causal Discovery with Observational and Interventional Data from Time-Series, Advanced Intelligent Systems.





Thank you! questions?