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Outline

Causal Discovery for Time-series Data • PCMCI algorithm

- Robotics Applications F-PCMCI algorithm CAnDOIT algorithm CausalFlow
 - ROS-Causal

The PC and FCI causal discovery methods work well with discrete/categorical data.

example

Smoker	Age	Lung cancer
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
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1	1	0
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non-smoker **0** - smoker **1** age under 50 **0** - age over 50 **1** no lung cancer **0** - lung cancer **1**

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The order is not important

Smoker	Age	Lung cancer
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5	1	0	1
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What if our data is time-dependent?



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The PC and FCI causal discovery methods work well with discrete/categorical data.

What if we deal with time-series data?

PC/FCI is inappropriate to use with time series data due to:

- time ordering
- lagged dependencies
- high false positive rates due to the autocorrelation

$$\begin{cases} X_t^0 = 0.2(X_{t-1}^1)^2 + \eta_t^0 \\ X_t^1 = \eta_t^1 \\ X_t^2 = 0.3(X_{t-2}^1)^2 + \eta_t^2 \end{cases}$$

$$\begin{array}{c} & & \\ & & & \\ & & \\ & & & \\ & & \\ & & & & \\ & & & \\ & & & & \\ & & & \\ & & & & \\ & & & \\ & & & & \\ & & &$$

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Robotics Applications
 F-PCMCI algorithm
 CAnDOIT algorithm
 CausalFlow
 ROS-Causal

It consists of two main steps:

• PC algorithm

retrieves the causal model structure by considering ONLY lagged dependencies as possible causal relationships between variables

• MCI test

validates the structure found at the previous step by performing a false positive rate optimisation control

 $X^i_{t- au} \perp\!\!\!\!\perp X^j_t | ilde{P}(X^i_{t- au}), ilde{P}(X^j_t)$

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$$\int egin{array}{l} X^0_t = 0.4 (X^1_{t-1})^2 + \eta \ X^1_t = n^1 \end{array}$$

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Main challenges in robotics:

- execution time of the causal discovery analysis
- conduct causal discovery using data from observations and interventions
- conduct the causal discovery analysis online



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PCMCI computational cost depends on:

- the length of the time-series
- the number of variables

Filtered-PCMCI (F-PCMCI) steps:

- takes in input a prefixed set of variables
- the Transfer Entropy-based filter analyses and removes irrelevant variables (e.g., constants or isolated ones). The reduced variable set is used to create a hypothetical causal model
- the hypothetical causal model needs to be validated by a proper causal analysis, which is performed by PCMCI

This strategy enables **faster** and **more accurate** causal discovery



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$$egin{cases} x_0(t) &= 2x_1(t-1) + 3x_3(t-1) + \eta_0 \ x_1(t) &= \eta_1 \ x_2(t) &= 1.1x_1(t-1)^2 + \eta_2 \ x_3(t) &= x_3(t-1) \cdot x_2(t-1) + \eta_3 \ x_4(t) &= x_4(t-1) + x_5(t-1) \cdot x_0(t-1) + \eta_4 \ x_5(t) &= \eta_5 \ x_6(t) &= \eta_6 \end{cases}$$



$$\begin{cases} x_{0}(t) = 2x_{1}(t-1) + 3x_{3}(t-1) + \eta_{0} \\ x_{1}(t) = \eta_{1} \\ x_{2}(t) = 1.1x_{1}(t-1)^{2} + \eta_{2} \\ x_{3}(t) = x_{3}(t-1) \cdot x_{2}(t-1) + \eta_{3} \\ x_{4}(t) = x_{4}(t-1) + x_{5}(t-1) \cdot x_{0}(t-1) + \eta_{4} \\ x_{5}(t) = \eta_{5} \\ x_{6}(t) = \eta_{6} \end{cases}$$
 F-PCMCI

 X_6

 X_1

PCMCI

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ight.$$
 Isolated



Considering the interaction scenario modelled by three variables

- v_{ii}: relative velocity between agent i and j
- d_{ii}: distance between agent i and j
- theta_{ii}: angle between agent i and j

Are all the observable variables useful to understand the observed scenario?









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• Observational data alone are often insufficient to accurately identify the correct causal model in complex scenarios where not all variables are observable

$$\begin{cases} X_0(t) = 0.9X_0(t-1) + 0.6X_1(t) + \eta_0 \\ L_1(t) = \eta_1 \\ X_2(t) = 0.9X_2(t-1) + 0.4X_1(t-1) + \eta_2 \\ X_3(t) = 0.9X_3(t-1) - 0.5X_2(t-2) + \eta_3 \end{cases}$$



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Causal model obtained by using Latent-PCMCI (LPCMCI): version of PCMCI, based on FCI, that handles latent variables



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Despite the "simple" toy problem (linear, 4 variables)

- reconstructing the causal model from data is never straightforward
- especially when there are hidden confounders

Causal model obtained by using Latent-PCMCI (LPCMCI): version of PCMCI, based on FCI, that handles latent variables



How can we perform causal discovery using data from observations 👀 and interventions 🔍?

- Observational data alone are often insufficient to accurately identify the correct causal model in complex scenarios where not all variables are observable
- We need interventions

CAnDOIT: CAusal Discovery with Observational 👀 and Interventional 🔦 data from Time-series



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CAnDOIT: CAusal Discovery with Observational 👀 and Interventional 🔨 data from Time-series



- For the observational case, we need to consider B's parents
- For the interventional case, we need to remove all incoming links to B

How can we enable a causal discovery method to do this?

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CAnDOIT: CAusal Discovery with Observational 👀 and Interventional 🔨 data from Time-series



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Castri, Luca, et al. "CAnDOIT: Causal Discovery with Observational and Interventional Data from Time Series" (2024).

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Causal model obtained by using CAnDOIT



Consider the brightness of the colours of the objects in the cylinder captured by a robot camera



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Consider the brightness of the colors of the objects in the cylinder captured by a robot camera

$$\begin{cases} F_c(t) = b(H(t-1)) \\ C_c(t) = b(H(t-1), v(t-1), d_c(t-1)) \end{cases}$$
$$b = K_h \frac{H}{H_{max}} + K_v \left(1 - \frac{v}{v_{max}}\right) + K_d \frac{d_c}{d_{c_{max}}}$$







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ROS-Causal

Robotics Applications CausalFlow





pip install
py-causalflow

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🍓 ROS-Causal

What is Robot Operating System (ROS)?





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Robotics Applications ROS-Causal



- ROS-Causal extracts and collects data from a HRI scenario, such as agents' trajectories, and performs causal analysis on the collected data in a batched manner. It is composed by four different rosnodes:
 - roscausal_robot
 - roscausal_human
 - roscausal_data
 - roscausal_discovery

Castri, Luca, et al. "Experimental Evaluation of ROS-Causal in Real-World Human-Robot Spatial Interaction Scenarios" (2024).

ROS-Causal_HRISim

HRI simulator involving:

- TIAGo robot
- pedestrians











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Reference

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- Castri, L., Mghames, S., Hanheide M. and Bellotto, N. 2024. CAnDOIT: Causal Discovery with Observational and • Interventional Data from Time-Series, Advanced Intelligent Systems.





Thank you! questions?



