# Enhancing Human-Robot Spatial Interaction through Causal Inference



Luca Castri, lcastri@lincoln.ac.uk PhD student University of Lincoln Website: *https://darko-project.eu* 

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## Outline

Motivation

Causal Inference overview

Causal Inference in Human-Robot Spatial Interaction



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#### Motivation

Causal Inference overview

Causal Inference in Human-Robot Spatial Interaction



• What is it?

## Science that studies the cause-and-effect relationship between events [Pearl, J., & Mackenzie, D. (2019). The book of why]



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## Science that studies the cause-and-effect relationship between events [Pearl, J., & Mackenzie, D. (2019). The book of why]

• It is divided into two main areas:



Causal Discovery starting from a set of variables (events) aims to reconstruct the cause-effect model underlying them

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## Motivation – robotics scenario





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Motivation - robotics scenario

Discovering the causal model will enable the robot to reason on it and to answer questions like:

- "what happens if I go this way?"
- "what would have happened if I remained still instead of moving?"





Motivation - robotics scenario

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take the best choice among possible HRSIs





## Outline

Motivation

#### **Causal Inference overview**

Causal Inference in Human-Robot Spatial Interaction



#### Science that studies the cause-and-effect relationship between events

- **Cause**: I never brush my teeth.
- **Cause**: I've smoked cigarettes daily for 20 years.

Effect: I have 5 cavities.

Effect: I have lung cancer.

#### Humans reason causally

• What about machines? They simply analyse data



• Performing NON-causal analysis on data can lead to wrong relationships

The cockcrow is **strongly** <u>associated</u> with sunrise



The ice cream sales is **strongly** <u>associated</u> with shark attacks





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## Correlation is not Causation



• What are we trying to discover? A **causal** graph data \_\_\_\_\_ causal graph

	X	Y	Z
0	20.000000	100.0	340.000000
1	20.204082	100.0	340.408163
2	20.408163	100.0	340.816327
3	20.612245	100.0	341.224490
4	20.816327	100.0	341.632653
2495	29.183673	300.0	958.367347
2496	29.387755	300.0	958.775510
2497	29.591837	300.0	959.183673
2498	29.795918	300.0	959.591837
2499	30.000000	300.0	960.000000



• What are we trying to discover? A **causal** graph Let's start from...

Undirected Graph



• What are we trying to discover? A **causal** graph Let's start from...

Undirected Graph



nodes

• What are we trying to discover? A **causal** graph Let's start from...

Undirected Graph



edges

• What are we trying to discover? A **causal** graph Let's start from...

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• What are we trying to discover? A **causal** graph

Undirected Graph



Directed Graph



• What are we trying to discover? A **causal** graph



• What are we trying to discover? A **causal** graph

Directed Graph

We do not want cycles



• What are we trying to discover? A **causal** graph

#### We do not want cycles

We need to guarantee the **acyclicity** assumption otherwise we can not distinguish between cause and effect

#### Directed Graph





• What are we trying to discover? A **causal** graph

#### Directed Acyclic Graph (DAG)



• Why "Direct"?

We need oriented edges otherwise they do not represent cause-and-effect relationships

• Why "Acyclic"?

We need to guarantee the **acyclicity** assumption otherwise we can not distinguish between cause and effect

• DAG configurations



• DAG configurations

Chain



A is a direct cause of B B is a direct cause of C

What about A and C?

• DAG configurations

#### Chain



association

A is a direct cause of B B is a direct cause of C

#### What about A and C?

They are associated (statistical dependent) through B

• DAG configurations

#### Chain



A is a direct cause of B B is a direct cause of C

#### What about A and C?

They are associated (statistical dependent) through B

If we condition on  $B \Rightarrow A$  and C are conditionally independent

By conditioning on B, we are creating a **blocked** path. If we do not condition on B, the path from A to C is **unblocked** and the association is free to flow.

• How can we discover a causal graph from observational data?



• How can we discover a causal graph from observational data?



• PCMCI algorithm

It consists of two main steps:

#### • PC algorithm

retrieves the causal model structure by considering ONLY lagged dependencies as possible causal relationships between variables

#### • MCI test

validates the structure found at the previous step by performing a false positive rate optimisation control

 $X^i_{t- au} \perp \!\!\!\!\perp X^j_t | ilde{P}(X^i_{t- au}), ilde{P}(X^j_t)$ 

Key parameter: au maximum time delay

Х

Y

Ζ
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### Outline

Motivation

Causal Inference overview







#### Aim

enable the robot to understand human behaviours by discovering the cause-effect relationship between events during a Human-Robot Spatial Interaction (HRSI)









**Single-agent scenario** system variables:

$$heta_g, d_g, v$$

expected cause-effect relationships:

 $egin{aligned} heta_g &= f( heta_g, d_g) \ d_g &= f(d_g, heta_g, v) \ v &= f(v, heta_g) \end{aligned}$ 

THÖR Dataset [A. Rudenko et al. 2020]

Multi-agent scenario system variables:

$$d_g, v, risk$$

expected cause-effect relationships:

$$egin{aligned} d_g &= f(d_g, v) \ v &= f(v, d_g, risk) \ risk &= f(risk, v) \end{aligned}$$
45

**THÖR** warehouse-like environment

ATC shopping centre



#### SCENARIO

D A T A S E T		Single-agent	Multi-agent
	THÖR	X	X
	ATC	X	

Different scenario observed from the same dataset ➡ different causal models

Same scenario observed from different datasets ➡ same causal models

Different scenario observed from different datasets ➡ different causal models



Different scenario observed from the same dataset ➡ different causal models







Single-agent

Same scenario observed from different datasets same causal models

# τ = 1







Same scenario observed from different datasets same causal models



Gaussian Process Regressor:

- supervised learning method designed to solve regression and probabilistic classification problems
- widely used for time-series prediction
- embedding the causal structure in the GPR  $\square$  Causal GPR





#### **Causal GPR approach**





#### **Causal GPR approach**





- Non-causal vs causal GPR comparison for the scenarios:
  - Single-agent (THÖR)
  - Single-agent (ATC)
  - Multi-agent (THÖR)

Mean NMAE	Single-agent		Multi-agent
	THÖR	ATC	THÖR
Non-causal GPR	0.21761	1.61692	0.37849
Causal GPR	0.1095	1.54552	0.36453

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Mean NMAE	Single-agent		Multi-agent
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Non-causal GPR	0.21761	1.61692	0.37849
Causal GPR	0.1095	1.54552	0.36453
~ -50%		~ -4%	
prediction error		prediction error	

#### Summing up

- First application of a causal discovery method to real-world sensor data for modelling HRSI
- New causal models from HRSI

#### Main limitation

• The PCMCI causal discovery is extremely demanding in terms of computational cost and hardware resources



L. Castri, S. Mghames, M. Hanheide, and N. Bellotto "Causal discovery of dynamic models for predicting human spatial interactions," in International Conference on Social Robotics (ICSR), 2022.



Can we speed up the causal discovery process?

#### Motivation

Causal analysis of complex and dynamical systems is extremely demanding in terms of time and hardware resources, making it a challenge for autonomous robotics with limited hardware resources and real-time requirements.

None of the state-of-the-art approaches extracts both the important features representing the system and the causal association between them, while at the same time taking into account the execution time and the computational cost for completing the task.





Can we speed up the causal discovery process?

# Are all the observable variables useful to understand the observed scenario?





Can we speed up the causal discovery process?

### Aim

Create an all-in-one algorithm able to:

- select the most meaningful features from a prefixed set of variables
- build a causal model from such selection

in order to enhance speed and accuracy of the causal discovery and make it more efficient and feasible for robotics applications.





Can we speed up the causal discovery process?

### **F-PCMCI steps**:

- takes in input a prefixed set of variables
- the Transfer Entropy-based filter analyses and removes irrelevant variables (e.g., constants or isolated ones). The reduced variable set is used to create a hypothetical causal model
- the latter needs to be validated by a proper causal analysis, which is performed by the PCMCI causal discovery algorithm

This strategy enables faster and more accurate causal discovery



Can we speed up the causal discovery process?

### **PCMCI vs F-PCMCI**

The correctness of our approach was evaluated based on toy problems with known ground-truth causal models. Various types of dependencies:

- linear and non-linear cross- and auto-dependency;
- noise-only equations;
- independent and dependent equations;
- different time-lag dependencies.

The analysis was carried out considering a number of system variables varying between 3 and 7. For each configuration, we performed 10 run tests with random system coefficients, using as evaluation metrics the mean over all the tests of:

- Structural Hamming Distance SHD;
- F1-score;
- execution time (in secs).



#### **Modeling Real-world Human Spatial Interactions**

We used our approach to model and predict spatial

interactions. This application involves three steps:

- extracting time-series of sensor data from human spatial interaction scenarios using the THÖR dataset;
- reconstruct the causal model using F-PCMCI;
- embedding the causal model in a LSTM-based prediction system.

In order to represent human spatial interactions, for each agent we considered 8 variables, which were then used in the causal analysis.



d <sub>g</sub>	distance to goal	$\boldsymbol{\theta}_{\mathbf{g}}$	angle to goal
V	velocity	Ø	angular velocity
risk	collision risk	<b>g</b> <sub>seq</sub>	goal position sequence
θ	orientation	d <sub>obs</sub>	distance to closest obstacle

**Modeling Real-world Human Spatial Interactions** 



PCMCI execution time 79'45"

F-PCMCI execution time 17'33"

#### **Modeling Real-world Human Spatial Interactions**





#### Summing up

• We extended and improved a state-of-the-art causal discovery algorithm, PCMCI, embedding an additional feature-selection module based on transfer entropy





#### Main limitation

• We are not exploiting the full power of causal inference: **the intervention** 

L. Castri, S. Mghames, M. Hanheide, and N. Bellotto, "Enhancing causal discovery from robot sensor data in dynamic scenarios," in Conference on Causal Learning and Reasoning, 2023.





#### Motivation

a primary limitation of the current state-of-the-art algorithms is that they can only handle observational data.

The latter are often insufficient to retrieve the correct causal model in complex scenarios where it is impossible to account for all the variables responsible for the system's evolution. In such cases, data from experiments, i.e. **interventional data**, are needed to eliminate spurious links and enhance the quality of the causal model

#### Example

Hidden confounder scenario



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71

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#### Example

Hidden confounder scenario



Performing an intervention on A, i.e. forcing its value:

- breaks the input links to A
- we can study the effect on C
- If varying A does not lead any change on C

A-C link is

spurious
## Thank you

## questions?



Luca Castri, lcastri@lincoln.ac.uk PhD student University of Lincoln

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